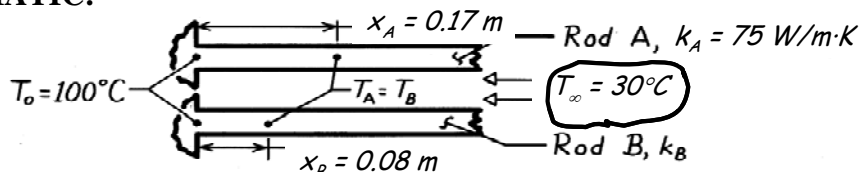


### PROBLEM 3.139

**KNOWN:** Positions of equal temperature on two long rods of the same diameter, but different thermal conductivity, which are exposed to the same base temperature and ambient air conditions.

**FIND:** Thermal conductivity of rod B,  $k_B$ .

**SCHEMATIC:**



**ASSUMPTIONS:** (1) Steady-state conditions, (2) Rods are infinitely long fins of uniform cross-sectional area, (3) Uniform heat transfer coefficient, (4) Constant properties.

**ANALYSIS:** The temperature distribution for the infinite fin has the form

$$\frac{\theta}{\theta_b} = \frac{T(x) - T_\infty}{T_o - T_\infty} = e^{-mx} \quad m = \left[ \frac{hP}{kA_c} \right]^{1/2}. \quad (1,2)$$

For the two positions prescribed,  $x_A$  and  $x_B$ , it was observed that

$$T_A(x_A) = T_B(x_B) \quad \text{or} \quad \theta_A(x_A) = \theta_B(x_B). \quad (3)$$

Since  $\theta_b$  is identical for both rods, Eq. (1) with the equality of Eq. (3) requires that

$$m_A x_A = m_B x_B$$

Substituting for  $m$  from Eq. (2) gives

$$\left[ \frac{hP}{k_A A_c} \right]^{1/2} x_A = \left[ \frac{hP}{k_B A_c} \right]^{1/2} x_B.$$

Recognizing that  $h$ ,  $P$  and  $A_c$  are identical for each rod and rearranging,

$$k_B = \left[ \frac{x_B}{x_A} \right]^2 k_A$$

$$k_B = \left[ \frac{0.08\text{ m}}{0.17\text{ m}} \right]^2 \times 75\text{ W/m}\cdot\text{K} = 16.6\text{ W/m}\cdot\text{K}.$$

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**COMMENTS:** This approach has been used as a method for determining the thermal conductivity. It has the attractive feature of not requiring power or temperature measurements, assuming of course, a reference material of known thermal conductivity is available.