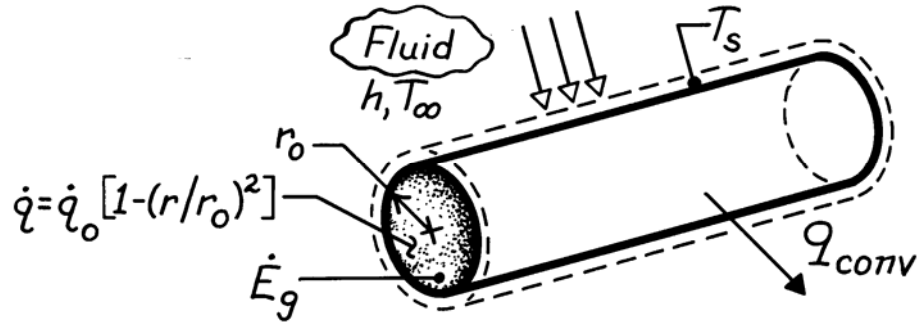


PROBLEM 1.44

KNOWN: Radial distribution of heat dissipation in a cylindrical container of radioactive wastes. Surface convection conditions.

FIND: Total energy generation rate and surface temperature.

SCHEMATIC:



ASSUMPTIONS: (1) Steady-state conditions, (2) Negligible temperature drop across thin container wall.

ANALYSIS: The rate of energy generation is

$$\begin{aligned}\dot{E}_g &= \int \dot{q} dV = \dot{q}_o \int_0^{r_o} \left[1 - (r/r_o)^2 \right] 2\pi r L dr \\ \dot{E}_g &= 2\pi L \dot{q}_o \left(r_o^2/2 - r_o^2/4 \right)\end{aligned}$$

or per unit length,

$$\dot{E}'_g = \frac{\pi \dot{q}_o r_o^2}{2}. \quad <$$

Performing an energy balance for a control surface about the container yields, at an instant,

$$\dot{E}'_g - \dot{E}'_{out} = 0$$

and substituting for the convection heat rate per unit length,

$$\begin{aligned}\frac{\pi \dot{q}_o r_o^2}{2} &= h(2\pi r_o)(T_s - T_\infty) \\ T_s &= T_\infty + \frac{\dot{q}_o r_o}{4h}. \quad <\end{aligned}$$

COMMENTS: The temperature within the radioactive wastes increases with decreasing r from T_s at r_o to a maximum value at the centerline.