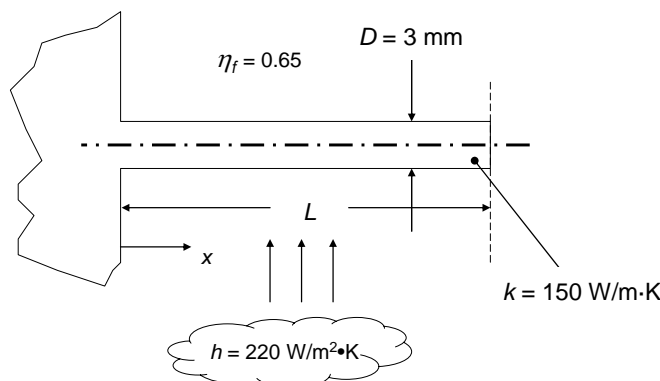


### PROBLEM 3.132

**KNOWN:** Thermal conductivity and diameter of a pin fin. Value of the heat transfer coefficient and fin efficiency.

**FIND:** (a) Length of fin, (b) Fin effectiveness.

**SCHEMATIC:**



**ASSUMPTIONS:** (1) Steady-state, one-dimensional conditions, (2) Negligible radiation heat transfer, (3) Constant properties, (4) Convection from fin tip.

**PROPERTIES:** *Given*, Aluminum Alloy:  $k = 150 \text{ W/m}\cdot\text{K}$ .

**ANALYSIS:** For an active fin tip, the efficiency may be expressed in terms of the corrected fin length as:

$$\eta_f = \frac{\tanh(mL_c)}{mL_c}$$

where  $m = \sqrt{hP/kA_c} = \sqrt{4h/kD} = \sqrt{4 \times 220 \text{ W/m}^2 \cdot \text{K} / (150 \text{ W/m} \cdot \text{K} \times 3 \times 10^{-3} \text{ m})} = 44.2 \text{ m}^{-1}$

Hence,  $\eta_f = 0.65 = \frac{\tanh(44.2 \text{ m}^{-1} \times L_c)}{44.2 \text{ m}^{-1} \times L_c}$  which may be solved by trial-and-error (or by using *IHT*) to yield  $L_c = 0.0303 \text{ m} = 30.3 \text{ mm}$ . The fin length is therefore,  $L = L_c - D/4 = 0.0303 \text{ m} - 0.003 \text{ m}/4 = 0.0296 \text{ m} = 29.6 \text{ mm}$ . <

The fin effectiveness is:

$$\begin{aligned} \varepsilon_f &= \frac{q_f}{hA_{c,b}\theta_b} = \frac{M \tanh(mL_c)}{hA_{c,b}\theta_b} = \frac{\sqrt{hPkA_{c,b}} \tanh(mL_c)}{hA_{c,b}} = \frac{2}{\sqrt{hD/k}} \tanh(mL_c) \\ &= \frac{2}{\sqrt{\frac{220 \text{ W/m}^2 \cdot \text{K} \times 3 \times 10^{-3} \text{ m}}{150 \text{ W/m} \cdot \text{K}}}} \tanh(44.2 \text{ m}^{-1} \times 30.3 \times 10^{-3} \text{ m}) = 26.3 < \end{aligned}$$

**COMMENTS:** The values of the fin effectiveness and fin efficiency are independent of the base or fluid temperatures.